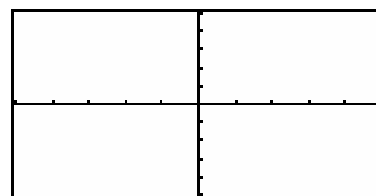


Assignment 16: Improper Integrals (6.6)
Please provide a handwritten response.

Name _____

1a. The integrals $\int_{-1}^1 \frac{1}{x} dx$ and $\int_{-1}^1 \frac{1}{x^2} dx$ are both improper and divergent. Sketch graphs of both $y = \frac{1}{x}$ and $y = \frac{1}{x^2}$ on the set of axes provided below. Be sure to label which graph is which.



$-1 \leq x \leq 1, -100 \leq y \leq 100$

1b. To try to evaluate $\int_{-1}^1 \frac{1}{x} dx$ on your calculator, use the **fnInt** command.

	TI-83 Plus/TI-84 Plus	TI-86
COMPUTE A DEFINITE INTEGRAL	MATH 9 fnInt The syntax is: (function,variable, low limit,high limit) This example is entered: fnInt(1/x,x,-1,1)	2ND ÷ (CALC) F5 (fnInt) The syntax is: (function,variable,low limit, high limit) This example is entered: fnInt(1/x,x,-1,1)

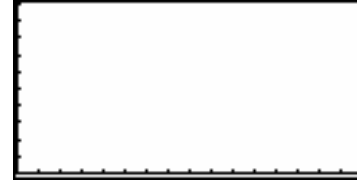
Record the result below. Does your calculator give you a value for this integral?

1c. Likewise evaluate $\int_{-1}^1 \frac{1}{x^2}$ by executing **fnInt(1/x²,x,-1,1)** and record the result below.

1d. Does your calculator confirm that each of these integrals is divergent? Explain carefully below why your calculator gives the results that it does.

2a. Sketch the graph of $f(x) = \frac{1}{\sqrt{1+\cos x}}$ over $0 \leq x \leq \pi$ on the axes provided below

and explain why the integral $\int_0^\pi \frac{1}{\sqrt{1+\cos x}} dx$ is improper.



$0 \leq x \leq \pi, 0 \leq y \leq 20$

2b. Execute the command `fnInt(1/(1+cos(x)),x,0,π)` and record the result below.
Does this integral converge?

2c. Execute the command `fnInt(1/(1+cos(x))^0.5,x,0,π)` and record the result below.
Does this integral converge?

2d. Execute the command `fnInt(1/(1+cos(x))^(1/2),x,0,π)` and record the result below.
Does this integral converge?